

Law of Sines Ambiguous Case

Date _____ Period _____

State the number of possible triangles that can be formed using the given measurements.

1) $m\angle A = 110^\circ, c = 19 \text{ cm}, a = 32 \text{ cm}$

2) $m\angle A = 131^\circ, a = 25 \text{ yd}, c = 8 \text{ yd}$

3) $m\angle B = 100^\circ, a = 33 \text{ km}, b = 29 \text{ km}$

4) $m\angle B = 61^\circ, a = 35 \text{ mi}, b = 32 \text{ mi}$

5) $m\angle A = 68^\circ, c = 34 \text{ yd}, a = 9 \text{ yd}$

6) $m\angle A = 57^\circ, c = 27 \text{ m}, a = 25 \text{ m}$

Solve each triangle. Round your answers to the nearest tenth.

7) $m\angle B = 27^\circ, a = 28 \text{ ft}, b = 18 \text{ ft}$

8) $m\angle C = 54^\circ, b = 24 \text{ km}, c = 23 \text{ km}$

$$9) \ m\angle A = 32^\circ, a = 17 \text{ cm}, c = 5 \text{ cm}$$

$$10) \ m\angle A = 52^\circ, c = 29 \text{ mi}, a = 27 \text{ mi}$$

$$11) \ m\angle B = 135^\circ, m\angle C = 6^\circ, b = 27 \text{ yd}$$

$$12) \ m\angle B = 34^\circ, m\angle C = 53^\circ, b = 14 \text{ mi}$$

$$13) \ m\angle A = 47^\circ, c = 34 \text{ mi}, a = 33 \text{ mi}$$

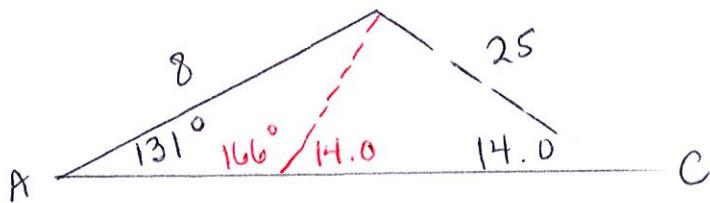
$$14) \ m\angle B = 12^\circ, m\angle C = 16^\circ, a = 34 \text{ km}$$

$$15) \ m\angle B = 24^\circ, m\angle C = 40^\circ, b = 19 \text{ km}$$

$$16) \ m\angle B = 64^\circ, a = 34 \text{ ft}, b = 33 \text{ ft}$$

Ambiguous Case WS

2. $m\angle A = 131^\circ$, $a = 25$ yds, $c = 8$ yds 1 triangle only



A 2nd Δ is NOT POSSIBLE.

$\begin{array}{l} 180^\circ \\ -131^\circ \\ \hline -166^\circ \end{array}$ The 3rd angle would need to be -117° in order to sum to 180° .

$\begin{array}{l} -166^\circ \\ -117^\circ \end{array}$

$$\frac{\sin 131^\circ}{25} = \frac{\sin C}{8}$$

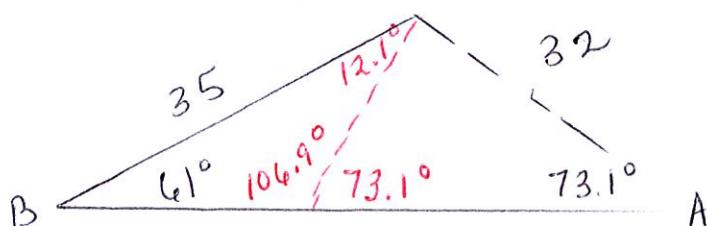
$$\sin C = \frac{8 \sin 131^\circ}{25}$$

$$C = \sin^{-1} \left(\frac{8 \sin 131^\circ}{25} \right)$$

$$C \approx 14.0$$

4. $m\angle B = 61^\circ$, $a = 35$, $b = 32$

2 triangles exist



$$\begin{array}{l} 180^\circ \\ -73.1^\circ \\ \hline 106.9^\circ \end{array}$$

$$\begin{array}{l} 180^\circ \\ -61^\circ \\ \hline 118.9^\circ \end{array}$$

$$\frac{\sin 61^\circ}{32} = \frac{\sin A}{35}$$

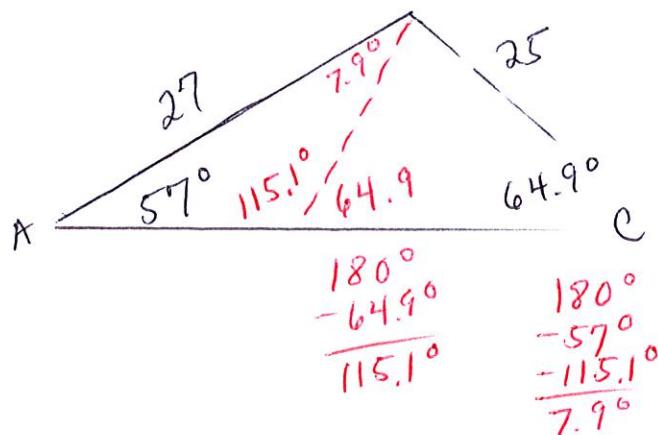
$$\sin^{-1} \left(\frac{35 \cdot \sin 61^\circ}{32} \right) = \sin A$$

A

$$A \approx 73.1^\circ$$

6. $m\angle A = 57^\circ, c = 27, a = 25$

2 triangles exist

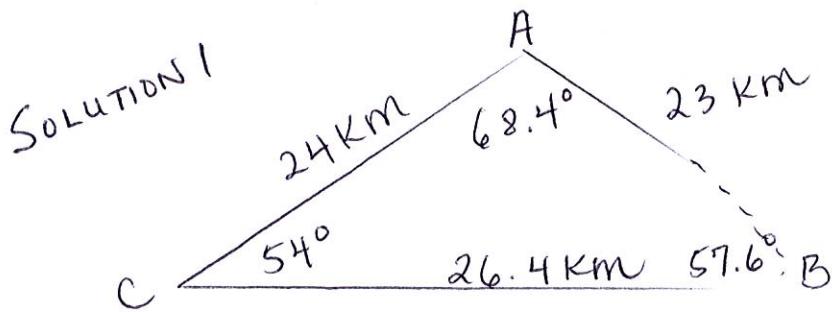


$$\frac{\sin 57^\circ}{25} = \frac{\sin C}{27}$$

$$\sin^{-1}\left(\frac{27 \sin 57^\circ}{25}\right) = \sin C$$

$$C \approx 64.9^\circ$$

8. $m\angle C = 54^\circ, b = 24 \text{ km}, c = 23 \text{ km}$



$$\frac{\sin 54^\circ}{23} = \frac{\sin 68.4^\circ}{a}$$

$$\frac{\sin 54^\circ}{23} = \frac{\sin B}{24}$$

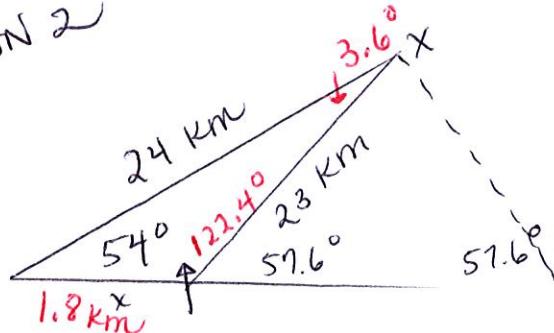
$$\sin^{-1}\left(\frac{24 \sin 54^\circ}{23}\right) \sin B$$

$$B \approx 57.6^\circ$$

$$a = \frac{23 \sin 68.4^\circ}{\sin 54^\circ}$$

$$a \approx 26.4$$

SOLUTION 2



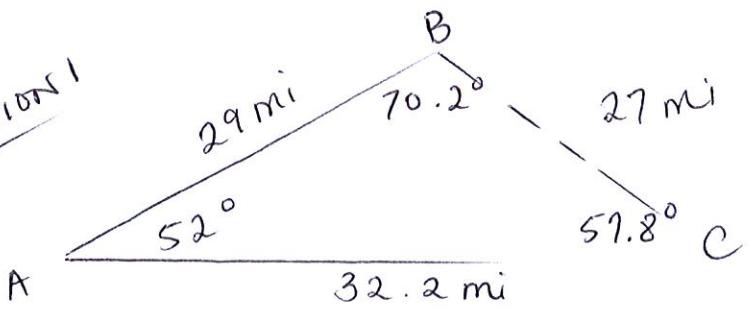
$$\frac{\sin 54^\circ}{23} = \frac{\sin 3.6^\circ}{x}$$

$$x = 23 \frac{\sin 3.6^\circ}{\sin 54^\circ}$$

$$x \approx 1.8 \text{ km}$$

10. $\text{mLA} = 52^\circ$, $c = 29 \text{ mi}$, $a = 27 \text{ mi}$

SOLUTION 1



$$\frac{\sin 52^\circ}{27} = \frac{\sin C}{29}$$

$$\sin^{-1}\left(\frac{29 \sin 52^\circ}{27}\right) = \sin C$$

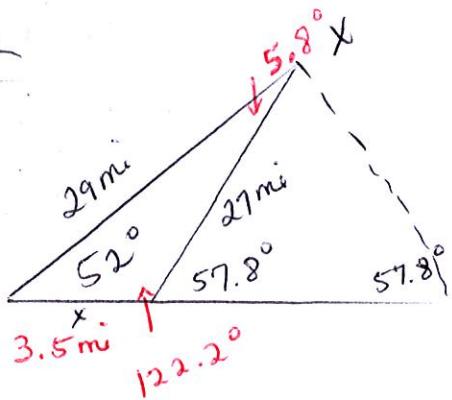
$$C \approx 57.8^\circ$$

$$\frac{\sin 52^\circ}{27} = \frac{\sin 70.2^\circ}{b}$$

$$b = \frac{27 \sin 70.2^\circ}{\sin 52^\circ}$$

$$b \approx 32.2$$

SOLUTION 2



$$\frac{\sin 52^\circ}{27} = \frac{\sin 5.8^\circ}{x}$$

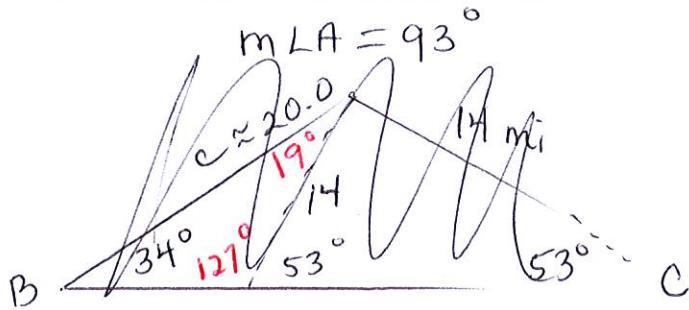
$$x = 27 \frac{\sin 5.8^\circ}{\sin 52^\circ}$$

$$x \approx 3.5$$

12.

$$\boxed{m\angle B = 34^\circ, m\angle C = 53^\circ, b = 14 \text{ mi}}$$

(AAS)



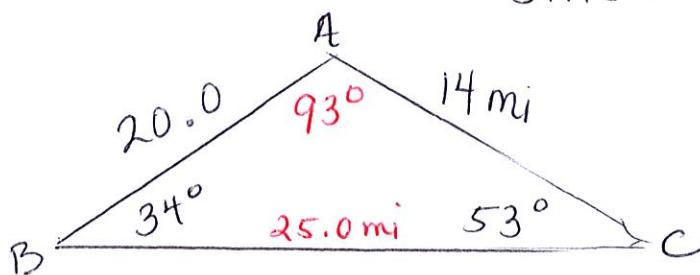
$$\frac{\sin 34^\circ}{14} = \frac{\sin 53^\circ}{c}$$

$$c = \frac{14 \sin 53^\circ}{\sin 34^\circ}$$

$$c \approx 20.0$$

$$\cancel{\frac{\sin 34^\circ}{14} = \frac{\sin 19^\circ}{x}}$$

$$x = \frac{14 \sin 19^\circ}{\sin 34^\circ}$$



$$\frac{\sin 34^\circ}{14} = \frac{\sin 93^\circ}{a}$$

$$a = 14 \frac{\sin 93^\circ}{\sin 34^\circ}$$

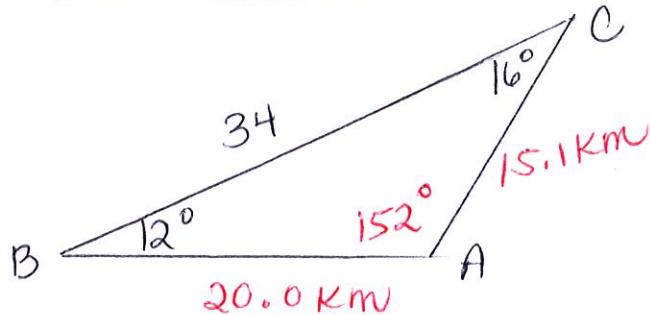
$$a \approx 25.0$$

There is no AMBIGUITY HERE. GIVEN ARE 2 ANGLES AND A SIDE! SIMPLY SOLVE FOR GIVEN A.

14. $m\angle B = 12^\circ$, $m\angle C = 16^\circ$, $a = 34 \text{ km}$

AAS

NO
NEED
TO
TEST



$$\frac{\sin 152^\circ}{34} = \frac{\sin 12^\circ}{b}$$

$$b = \frac{34 \sin 12^\circ}{\sin 152^\circ}$$

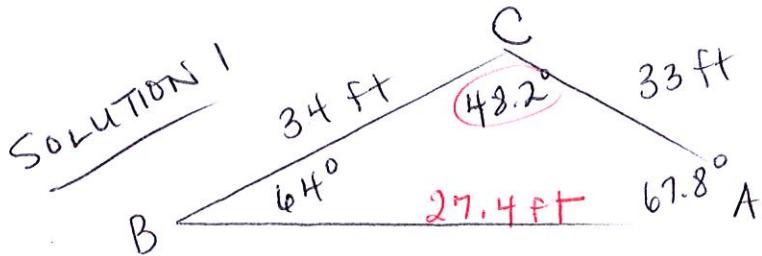
$$b \approx 15.1$$

$$\frac{\sin 152^\circ}{34} = \frac{\sin 16^\circ}{c}$$

$$c = \frac{34 \sin 16^\circ}{\sin 152^\circ}$$

$$c \approx 20.0$$

16. $m\angle B = 64^\circ$, $a = 34 \text{ ft}$, $b = 33 \text{ ft}$



$$\frac{\sin 64^\circ}{33} = \frac{\sin A}{34}$$

$$\sin^{-1} \left(\frac{34 \sin 64^\circ}{33} \right) = \sin A$$

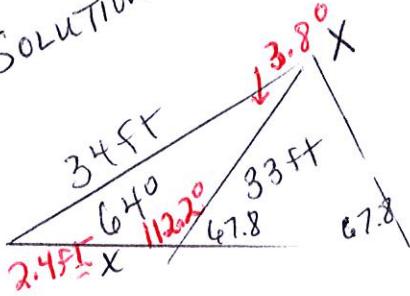
$$A \approx 67.8^\circ$$

$$\frac{\sin 64^\circ}{33} = \frac{\sin 48.2^\circ}{c}$$

$$c = \frac{33 \sin 48.2^\circ}{\sin 64^\circ}$$

$$c \approx 27.4$$

SOLUTION 2



$$\frac{\sin 64^\circ}{33} = \frac{\sin 3.8^\circ}{x}$$

$$x = \frac{33 \sin 3.8^\circ}{\sin 64^\circ}$$

$$x \approx 2.4$$

