

X IS SQUARED VERTICAL PARABOLAS

$y = x^2$ parent function
 QUADRATIC
 $y = -x^2$

Standard form: $y = \frac{1}{4p}(x-h)^2 + k$
 ↑ (h, k)

Complete the table.

Equation of parabola	Does it open up or down?	vertex	p value
$y = -\frac{1}{28}(x-5)^2 - 8$	opens downward (negative LC) ↓	(5, -8)	$4p = 28$ $p = 7$
$y = \frac{1}{4}(x+3)^2 + 7$	↑ LC is positive	(-3, 7)	$4p = 4$ $p = 1$
$y = \frac{1}{8}x^2 + 1$ $\frac{1}{8}(x+0)^2 + 1$	↑	(0, 1)	$4p = 8$ $p = 2$
$y = -\frac{1}{20}(x-6)^2 - 11$	↓	(6, -11)	$4p = 20$ $p = 5$

distance from vertex to focus

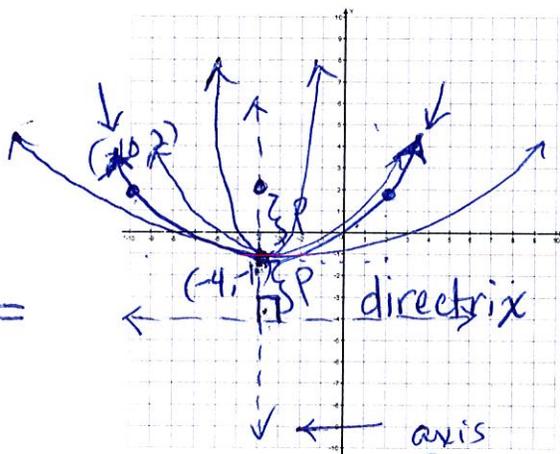
Graph the following parabolas.

- Determine the direction of opening
- Determine the vertex
- Calculate the value of p
- Plot the vertex ✓
- Use the p value to plot the focus and the directrix. ✓
- Use an x/y table to determine at least two more points on the graph. Use symmetry to draw the other two.
- Sketch the curve



EX 1 $y = \frac{1}{12}(x+4)^2 - 1$

Analysis
 $(1 \div 12)$
 $v: (-4, -1)$

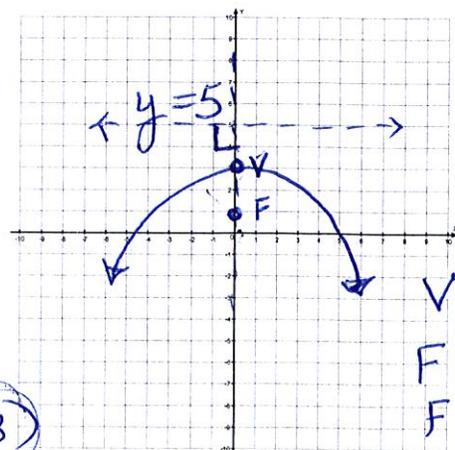


$4p = 12$
 $p = 3$
 focus
 (-4, -1 + 3)
 (-4, 2)
 directrix
 (-4, -1 - 3)

axis of symmetry
 $y = -4$ is the directrix

EX 2 $y = -\frac{1}{8}x^2 + 3$

Vertex
 (0, 3) ↓



$4p = 8$
 $p = 2$
 $V: (0, 3)$
 $F: (0, 3 - 2)$
 $F: (0, 1)$

directrix: $y = 5$

HORIZONTAL PARABOLAS

Standard form: $x = \frac{1}{4p}(y-k)^2 + h$

If y is squared, it's horizontal

positive →

$$x = y^2$$

← LEFT

Complete the table.

Equation of parabola	Does it open left or right?	vertex	p value
$x = \frac{1}{8}y^2 + 5$	→	(5, 0)	$4p = 8$ $p = 2$
$x = \frac{1}{32}(y+2)^2 + 0$	→	(0, -2)	$4p = 32$ $p = 8$
$x = -\frac{1}{16}(y-9)^2 - 7$	←	(-7, 9)	$4p = 16$ $p = 4$
$x + 3 = -\frac{1}{4}(y+1)^2$ $x = -\frac{1}{4}(y+1)^2 - 3$	←	(-3, -1)	$4p = 4$ $p = 1$

Graph the following parabolas.

- Determine the direction of opening
- Determine the vertex
- Calculate the value of p
- Plot the vertex
- Use the p value to plot the focus and the directrix.
- Use an x/y table to determine at least two more points on the graph. Use symmetry to draw the other two.
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HORIZONTAL → ←

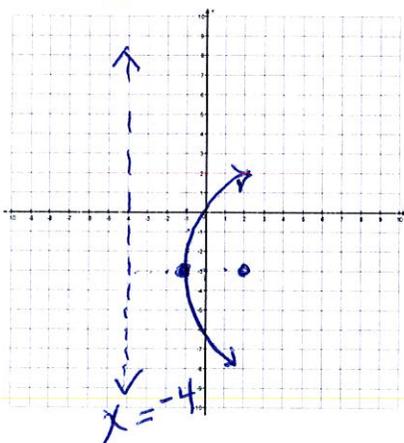
EX 1 $x = \frac{1}{12}(y+3)^2 - 1$

V: (-1, -3)

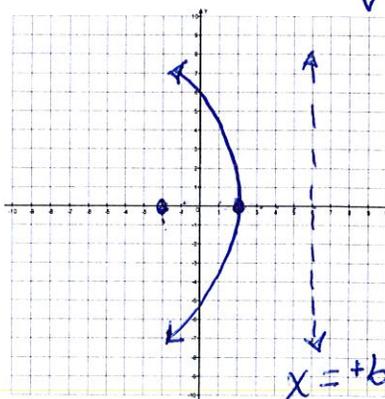
EX 2

$x = -\frac{1}{16}y^2 + 2$

V: (2, 0)



$4p = 12$
 $p = 3$
(+3 (right))
(-1, -3)
focus: (2, -3)
directrix: $x = -4$



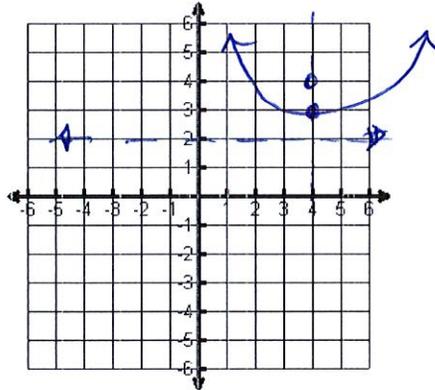
$4p = 16$
 $p = 4$
focus: (-2, 0)

Extra practice on parabolas

Give the direction, vertex, p, focus, directrix, and graph

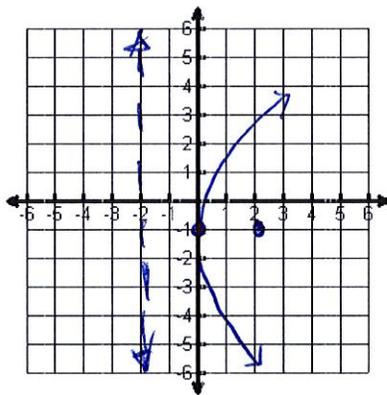
Analysis

1. $y = \frac{1}{4}(x - 4)^2 + 3$



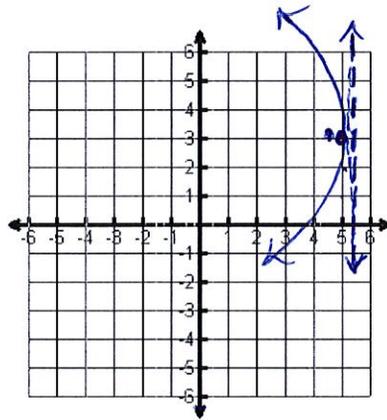
↑
 $v: (4, 3)$ $p = 1$
 focus $(4, 4)$
 directrix: $y = 2$

2. $x = \frac{1}{8}(y + 1)^2$



→ $v: (0, -1)$
 $p = 2$
 focus $(2, -1)$
 directrix:
 $x = -2$

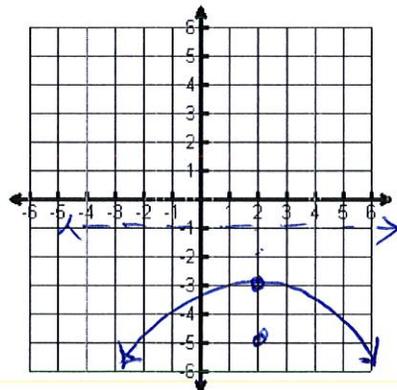
3. $x = -(y - 3)^2 + 5$



← $v (5, 3)$
 $4p = -1$
 $p = -\frac{1}{4}$
 focus $(4.75, 3)$
 directrix: $x = 5.25$

4. $y = -\frac{1}{8}(x - 2)^2 - 3$

$y = x^2$ $y = x^2$ $y = -x^2$



↓ $(2, -3)$ is vertex
 $p = 2$
 focus $(2, -5)$
 directrix: $y = -1$

$$5. y+1 = \frac{1}{16}(x+3)^2$$

$$y = \frac{1}{16}(x+3)^2 - 1$$

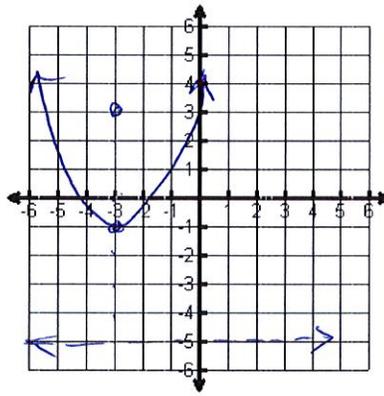
↑ $(-3, -1)$ Vertex

$$4p = 16$$

$$p = 4$$

focus : $(-3, 3)$

directrix : $y = -5$



$$6. x-2 = -\frac{1}{12}(y+1)^2$$

$$x = -\frac{1}{12}(y+1)^2 + 2$$

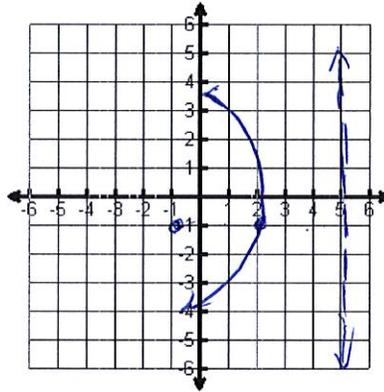
← vertex $(2, -1)$

$$4p = 12$$

$$p = 3$$

focus $(-1, -1)$

directrix : $x = 5$



Put into standard form. Then do all the stuff from 1st page.

$$5. x^2 + 2x - 4y + 9 = 0$$

Isolate x or y

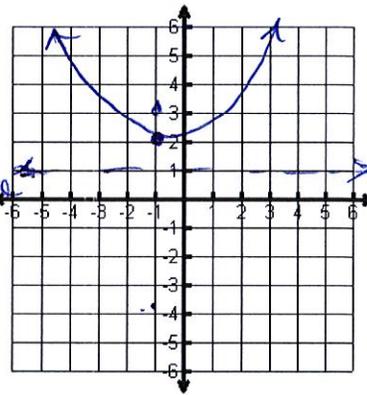
$$x^2 + 2x + 9 = 4y$$

$$4y = x^2 + 2x + 9$$

$$4y = (x^2 + 2x + 1) + 8$$

$$\frac{4y}{4} = \frac{(x+1)^2 + 8}{4}$$

← Keep balance



V : $(-1, 2)$
 $p = 1$
 focus $(-1, 3)$
 directrix
 $y = 1$

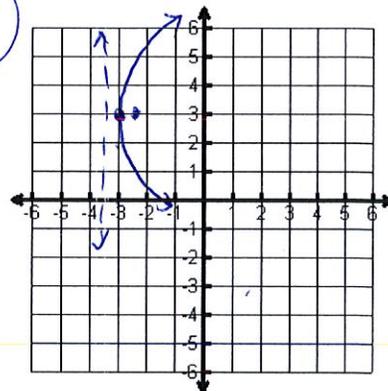
$$6. x^2 - 6y - 2x + 3 = 0$$

$$y^2 - 6y + 3 = 2x$$

$$2x = (y^2 - 6y + 9) + 3 - 9$$

$$\frac{2x}{2} = \frac{(y-3)^2 - 6}{2}$$

$$x = \frac{1}{2}(y-3)^2 - 3$$



V : $(-3, 3)$
 $p = \frac{1}{2}$
 $4p = 2$
 $p = \frac{1}{2}$

Focus $(-2.5, 3)$
 directrix :
 $x = -3.5$

Puzzle
Worksheet
writing
equations

1. $y = x^2 - 2x - 2$

$$y = (x^2 - 2x + \quad) - 2$$

$$y = (x^2 - 2x + 1) - 2 - 1$$

↑ ↑

balance by adding
opposites on some side
of equation

$$y = (x - 1)^2 - 3$$

2. $y = x^2 + 12x + 17$

$$y = (x^2 + 12x + 36) + 17 - 36$$

$$y = (x + 6)^2 - 19$$

3. $y = 2x^2 - 8x - 3$

$$y = 2(x^2 - 4x + 4) - 3 - 8$$

$$y = 2(x - 2)^2 - 11$$

4. $y = -5x^2 + 10x + 23$

$$y = -5(x^2 - 2x + 1) + 23 + 5$$

$$y = -5(x - 1)^2 + 28$$

$$5. \quad 2y = x^2 - 6x + 13$$

$$2y = (x^2 - 6x + 9) + 13 - 9$$

$$2y = (x-3)^2 + 4$$

$$y = \frac{1}{2}(x-3)^2 + 2$$

$$6. \quad x^2 - 4x - 3y + 1 = 0$$

$$x^2 - 4x + 1 = 3y$$

$$3y = x^2 - 4x + 1$$

$$3y = (x^2 - 4x + 4) + 1 - 4$$

$$3y = (x-2)^2 - 3$$

$$y = \frac{1}{3}(x-2)^2 - 1$$

$$7. \quad x^2 + 10x + 2y - 3 = 0$$

$$2y = -x^2 - 10x + 3$$

$$2y = -(x^2 + 10x + 25) + 3 + 25$$

$$2y = -(x+5)^2 + 28$$

$$y = -\frac{1}{2}(x+5)^2 + 14$$

$$8. \quad 5y + 4 = 6x^2 - 12x$$

$$5y = 6x^2 - 12x - 4$$

$$5y = 6(x^2 - 2x + 1) - 4 - 6$$

$$5y = 6(x-1)^2 - 10$$

$$y = \frac{6}{5}(x-1)^2 - 2$$

$$9. \quad 6x^2 + 5y - 25 = 0$$

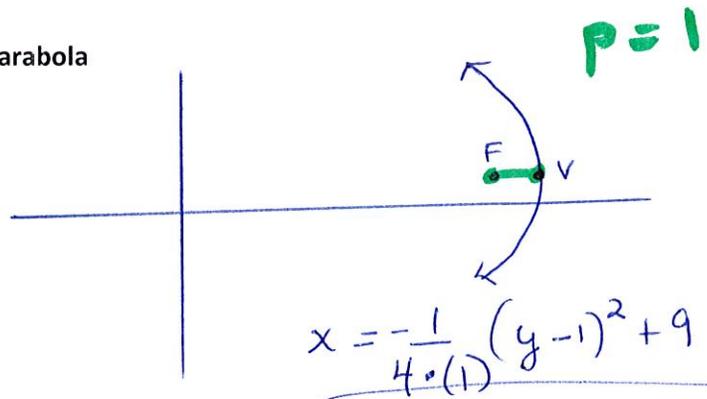
$$5y = -6x^2 + 25$$

$$y = -\frac{6}{5}x^2 + 5$$

Use the information to write the equation of the parabola

7. Vertex (9,1), Focus (8,1)

7.



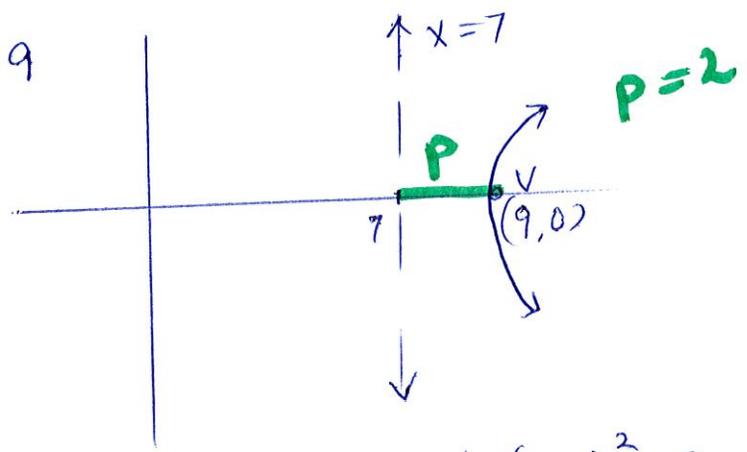
$$x = -\frac{1}{4 \cdot (1)} (y-1)^2 + 9$$

$$y = -\frac{1}{4} (y-1)^2 + 9$$

8. Vertex (-4,3) Focus (-5,3)

9. Vertex (9,0) Directrix x = 7

9.



$$x = \frac{1}{4 \cdot 2} (y-0)^2 + 9$$

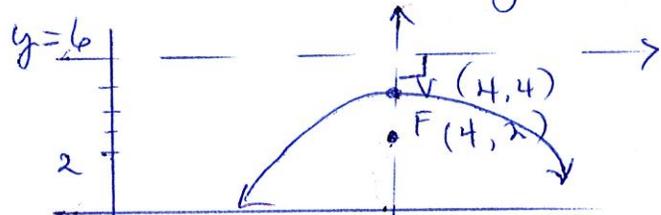
$$x = \frac{1}{8} y^2 + 9$$

10. Vertex (-3,3) Directrix x = 1

11. Focus (4,2) Directrix y=6

12. Focus (3,2) Directrix y = 0

11. focus (4,2)
directrix: y=6



distance from focus to directrix is 4. ∴ distance p = 2

vertex lies halfway between focus + directrix

$$y = -\frac{1}{8} (x-4)^2 + 4$$