

Name _____

Systems of Conics – Circle and a Line

Solve each system

$$1. \begin{aligned} x^2 + y^2 &= 5 \\ y &= -2x \end{aligned}$$

$$x^2 + (-2x)^2 = 5$$

$$x^2 + 4x^2 = 5$$

$$5x^2 = 5$$

$$x^2 = 1$$

$$x = \pm 1$$

2 solutions
 $\boxed{(1, -2)}$
 $\boxed{(-1, 2)}$

$$3. \begin{aligned} (x-1)^2 + y^2 &= 9 \\ y &= 3 \end{aligned}$$

$$(x-1)^2 + 3^2 = 9$$

$$x^2 - 2x + 1 + 9 = 9$$

$$x^2 - 2x + 1 = 0$$

$$(x-1)(x-1) = 0$$

$$x = 1$$

$$5. \begin{aligned} x^2 + y^2 &= 18 \\ x - y &= 0 \\ \rightarrow x &= y \end{aligned}$$

$$x^2 + x^2 = 18$$

$$2x^2 = 18$$

$$x^2 = 9$$

$$x = \pm 3$$

2 solutions
 $\boxed{(1, -2)}$
 $\boxed{(-1, 2)}$

$$2. \begin{aligned} x^2 + y^2 &= 49 \\ y &= x - 7 \end{aligned}$$

$$x^2 + (x-7)^2 = 49$$

$$x^2 + x^2 - 14x + 49 = 49$$

$$2x^2 - 14x = 0$$

$$2x(x-7) = 0$$

$$2x = 0 \quad x-7 = 0$$

$$x = 0, \quad x = 7$$

$$4. \quad (x+3)^2 + (y-1)^2 = 1$$

$$\begin{aligned} x-3y &= 3 \\ \rightarrow x &= 3+3y \end{aligned}$$

NO SOLUTION
 DOES NOT FACTOR
 discriminant
 negative

$$(3+3y+3)^2 + (y-1)^2 = 1 \quad \text{negative}$$

$$(3y+6)^2 + (y-1)^2 = 1$$

$$(3y+6)(3y+6) + (y-1)(y-1) = 1$$

$$9y^2 + 18y + 36 + y^2 - 2y + 1 = 1$$

$$10y^2 + 34y + 36 = 0$$

$$2(5y^2 + 17y + 18) = 0$$

~~90~~
~~17~~

$$x^2 + (x+1)^2 = 25$$

$$x^2 + (x+1)(x+1) = 25$$

$$x^2 + x^2 + 2x + 1 = 25$$

$$2x^2 + 2x - 24 = 0$$

$$2(x^2 + x - 12) = 0$$

$$2(x+4)(x-3) = 0 \rightarrow x = -4 \quad x = 3$$

$\boxed{(-4, -3)}$
 $\boxed{(3, 4)}$

$$x - 3y = 3 \rightarrow x = 3 + 3y$$

$$(x+3)^2 + (y-1)^2 = 1$$

$$(3 + 3y + 3)^2 + (y-1)^2 = 1$$

$$(6 + 3y)^2 + (y-1)^2 = 1$$

$$(6 + 3y)(6 + 3y) + (y-1)(y-1) = 1$$

$$36 + 18y + 18y + 9y^2 + y^2 - y - y + 1 = 1$$

$$10y^2 + 34y + 37 = 0$$

$$10y^2 + 34y + 36 = 0$$

$$x = \frac{-34 \pm \sqrt{34^2 - 4(10)(36)}}{2(10)}$$

$$x = \frac{-34 \pm \sqrt{-284}}{20} \leftarrow \begin{matrix} \text{NO REAL} \\ \text{SOLUTION} \end{matrix}$$